

1. Taking your Chance

1.1. Probability Rules

PROBABILITY (of an event): ratio of number of cases favorable to number of all cases possible, when nothing leads us to expect that any one of these cases should occur more than any other, which renders them, for us, equally possible.

Key concepts: SAMPLE SPACE, EVENT, COMBINING EVENTS, INDEPENDENCE

1.2. Conditional Probabilities

CONDITIONAL PROBABILITY (of an event A given an event B):

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

Key concepts: DEPENDENCE, CONDITIONAL PROBABILITY

1.3. Bayes' Theorem

BAYES' THEOREM:

$$P(A|B) = \frac{P(B|A) \cdot P(A)}{\sum_{i=1}^n P(B|A_i) \cdot P(A_i)}$$

Key concepts: TOTAL PROBABILITY RULE, SENTIMENT ANALYSIS, BAYES' THEOREM

2. Are you able to Recognize your Sentiment from your Sentence?

2.1. Birthday Paradox

TASKS:

- **TASK 1&2:** Create and apply the function `generate_birthdays(n)` to one of the following values of n :
[5, 10, 15, 25, 30, 35, 40, 45, 50, 75, 100]
- **TASK 3 (Optional)** Apply the function `generate_birthdays(n)` to all the sizes above.
- **TASK 4&5:** Create and apply the function `has_duplicate(birthdays)` for the chosen group size.
- **TASK 6:** Conduct a simulation study for the chosen group size.
- **TASK 7 (Optional)** Conduct a **simulation study** for all the sizes above.
- **TASK 8:** Answer the questions!

Key concepts: FOR LOOP, CONDITIONALS, SIMULATION STUDY

2.2. Conditional Probabilities & Videogames

IN THE DIGITAL REALM OF CYBERVALE, SARAH, A BRAVE HACKER, VENTURES INTO THE TREACHEROUS DARKNET. THIS NETWORK IS FRAUGHT WITH DANGERS, FROM ENCRYPTED TRAPS TO LURKING DIGITAL PREDATORS. AS SHE JOURNEYS THROUGH, SARAH DISCOVERS THAT 40% OF THE PATHWAYS LEAD TO REGIONS INFESTED WITH MALICIOUS CODE, POSING IMMINENT THREATS (THERE, THE PROBABILITY OF ENCOUNTERING A MALWARE IS 90%). IN A SECURE REGION ONLY 5% OF ENCOUNTERED OBJECTS ARE MALWARE. ADDITIONALLY, WITHIN SECURE SECTORS, THERE'S A 25% CHANCE THAT SARAH WILL FIND A POWERFUL ANTIVIRUS PROGRAM, OFFERING HER CRUCIAL DEFENSE. UNFORTUNATELY, IN INFECTED AREAS, THE PROBABILITY OF FINDING SUCH A PROGRAM DROPS TO A MERE 15%. GIVEN THE TYPE OF REGION (SECURE OR INFECTED), FINDING THE ANTIVIRUS AND ENCOUNTERING A MALWARE CAN BE CONSIDERED INDEPENDENT EVENTS.

TASKS:

- **TASK 9:** Translate the videogame in probability terms
- **TASK 10:** Answer the questions!
- **TASK 11&12:** Design your videogame by writing and applying the function `sarahs_journey()`;

Key concepts: EXPLAIN REAL PROBLEMS VIA PROBABILITIES

2.3. Sentiment Analysis

SENTIMENT ANALYSIS: aimed at computing probability of positive (or negative) sentiment given a sentence of n words.

TASKS:

- **TASK 13-16:** Load datasets using `load_dataset(file_path)`; merge difference sources; divide positive & negative;
- **TASK 17&18:** Build your sentiment dictionary (probability of the word in a positive/negative context);
- **TASK 19&20:** Create and apply `calculate_sentiment_probability` to compute the sentiment given a sentence;
- **TASK 21:** Have fun with the last function: **Are you able to Recognize your Sentiment from your Sentences?**

Key concepts: SENTIMENT RANDOM VARIABLE, WORD RANDOM VARIABLE, SENTIMENT DICTIONARY

3. Markov Chains

TASK: Make a haiku by each choosing one word after hearing what previous person has chosen.

3.1. Markov Chain: Definition

MARKOV CHAIN: stochastic process that only looks at last state to decide where to go next.

$$P(X_{n+1} = x_n | X_0 = x_0, X_1 = x_1, \dots, X_n = x_n) = P(X_{n+1} = x_n | X_n = x_n)$$

Key concepts: STATE, MARKOV CHAIN, MARKOV PROPERTY, CHESS AS MARKOV CHAIN, RANDOM WALK

3.2. Transition Probabilities

TRANSITION MATRIX: matrix $P = [p_{ij}]$ such that:

$$p_{ij} = P(X_{n+1} = j | X_n = i)$$

The rows of a transition matrix adds up to 1.

Key concepts: TRANSITION PROBABILITIES, STATE SPACE, TIME STRUCTURE

3.3. Limiting Probabilities

CHAPMAN-KOLMOGOROV THEOREM:

$$P_{ij}^{(n)} = (P^n)_{ij}$$

Key concepts: INFECTION DISEASES MODEL, FINANCIAL MARKET MODEL, LEHRER-WAGNER MODEL, LIMITING DISTRIBUTION, RECURRENCE, FOREST FIRE SIMULATION

3.4. Text Generation using Markov Chains

$$p_{ij} = \frac{\text{\# instances of word i followed by word j}}{\text{\# instances of word i}}$$

Key concepts: MODEL TRAINING, TEXT GENERATION, ADVANCED TEXT GENERATION

4. Are you Able to Write like... Oscar Wilde?

4.1. Who do you want to Resemble as a Writing Style?

TASKS:

- **TASK 1&2:** Create and apply the function `read_text_file(filename)` to load the Oscar Wilde (OW)'s book and *Green Eggs and Ham* by Dr. Seuss.
- **TASK 3:** Read and apply the function `preproc(canon, letter, delimit, remov)` to above mentioned texts.

Key concepts: LOADING DATA, PRE-PROCESSING STEP

4.2. Time for Markov Chains

- **TASK 4&5:** Create and apply the function `transition(canon)` to the text *Green Eggs and Ham*. Use the function `transition_row_for_word(word, transition_matrix, words)` to answer the questions.
- **TASK 6:** Read the code to exploit networks to visualize the transition probabilities.
- **TASK 7:** Answer the questions!

Key concepts: TRANSITION MATRIX IN PRACTICE, NETWORK VISUALIZATION OF TRANSITION PROBABILITIES, IRREDUCIBLE MARKOV CHAINS

4.3. Let us work... Step by Step!

Our final goal (if we opt for a depth equal to 2):

$$P(W_3 = w | W_1 = w_1, W_2 = w_2)$$

By means of a function named `writer`.

- **TASK 8&9:** Create and apply the function `initialize_novel(canon, depth, seed, n_tot)` to the OW text with depth equal to 3, without or with a seed provided.
- **TASK 10&11:** Create and apply the function `get_candidates(canon, novel, temp_depth, n_tot)` to the output obtained before.
- **TASK 12&13:** Create and apply the function `choose_next_word(canon, select)` to the output obtained before.
- **TASK 14&15:** Create and apply the function `generate_sentence(canon, novel, depth, n_tot)` to the output obtained before.
- **TASK 16:** Read the function `format_sentences(novel, delimit)` to deal with punctuation.
- **TASK 17:** Put the pieces together by writing the function `writer(canon)`.

Key concepts: FUNCTION COMPOSITION

4.4. Space for Imagination!

Use the function `writer(canon)` to write like... Oscar Wilde!